

TABLE OF CONSTANTS

CONSTANT	SYMBOL	VALUE
speed of light in a vacuum	c	$3.00 \times 10^8 \text{ m s}^{-1}$
gravitational constant	G	$6.673 \times 10^{-11} \text{ N m}^2 \text{ kg}^{-2}$
orbital constant	$G M_E$	$3.986 \times 10^{14} \text{ m}^3 \text{ s}^{-2}$
standard gravitational acceleration	g	9.81 m s^{-1}
Planck's constant	h	$6.626 \times 10^{-34} \text{ J s}$
Boltzmann's constant	k	$1.381 \times 10^{-23} \text{ J K}^{-1}$
first radiation constant	c_1	$1.191 \times 10^{-16} \text{ W m}^2 \text{ sr}^{-1}$
second radiation constant	c_2	$1.439 \times 10^{-2} \text{ m K}$
Stefan-Boltzmann constant	σ	$5.670 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$
Wien's displacement law constant	none	$2.8979 \times 10^{-3} \text{ m K}$
Avogadro's number	N_A	$6.022 \times 10^{23} \text{ molecules mole}^{-1}$
Dobson unit	DU	$1 \text{ DU} = 2.687 \times 10^{16} \text{ molecules/cm}^2$
molar gas constant	R	$8.3143 \text{ J mole}^{-1} \text{ K}^{-1}$
angular velocity of Earth	$d\Omega_E / dt$	$7.292 \times 10^{-5} \text{ rad s}^{-1}$
solar day	T_{solar}	86,400 s
sidereal day	T_{sidereal}	86,164.1 s
mean radius of Earth	R_E	$6.371 \times 10^6 \text{ m} = 6371 \text{ km}$
mass of Earth	M_E	$5.9737 \times 10^{24} \text{ kg}$
standard pressure	p_0	$1013.25 \text{ mbar} = 1.01325 \times 10^5 \text{ N m}^{-2}$
standard temperature	T_0	273.15 K
scale height of Earth's atmosphere	$H = RT/Mg$	$\sim 7 \text{ km}$
radius of Sun (visible disk)	R_{sun}	$6.96 \times 10^8 \text{ m}$
mean Earth-Sun distance	d_{sun}	$1.50 \times 10^{11} \text{ m}$
solar constant	S_{sun}	1368 W m^{-2}
molecular mass of CO ₂	M	$44 \text{ g/mole} = 7.3065 \times 10^{-26} \text{ kg/molecule}$
molecular mass of H ₂ O	M	$18 \text{ g/mole} = 2.9890 \times 10^{-26} \text{ kg/molecule}$
molecular mass of O ₂	M	$32 \text{ g/mole} = 5.3138 \times 10^{-26} \text{ kg/molecule}$

LIST OF EQUATIONS

$$\begin{aligned}
F &= \frac{Gm_1 m_2}{r^2} & T &= 2\pi \sqrt{\frac{r^3}{Gm_E}} & v &= \sqrt{Gm_E \left(\frac{2}{r} - \frac{1}{a} \right)} & r &= \frac{a(1-\varepsilon^2)}{1+\varepsilon \cos \theta} \\
M &= e - \varepsilon \sin e = n(t - t_p) & \cos \theta &= \frac{\cos e - \varepsilon}{1 - \varepsilon \cos e} & \cos e &= \frac{\cos \theta + \varepsilon}{1 + \varepsilon \cos \theta} & \tilde{T} &= \frac{2\pi}{\bar{n} + \frac{d\omega}{dt}}
\end{aligned}$$

$$\begin{aligned}
LT &= UT + \frac{\psi}{15^\circ} & ECT &= UT + \frac{\psi_N}{15^\circ} = 12 + \frac{\Delta \psi}{15^\circ} & \vec{S} &= c^2 \varepsilon_0 \vec{E} \times \vec{H} \\
I &= \int_0^\infty I_\lambda d\lambda = \int_0^\infty I_\nu d\nu = \int_0^\infty I_{\bar{\nu}} d\bar{\nu} & B_\lambda &= \frac{2hc^2 \lambda^{-5}}{\exp\left(\frac{hc}{\lambda kT}\right) - 1} = \frac{c_1 \lambda^{-5}}{\exp\left(\frac{c_2}{\lambda T}\right) - 1}
\end{aligned}$$

$$\begin{aligned}
\lambda_{\max} (\mu m) &= \frac{2897.9}{T(K)} & M_{BB} &= \sigma T^4 & B_\lambda &\cong \frac{c_1 T}{c_2 \lambda^4} & \alpha_\lambda + R_\lambda + \tau_\lambda &= 1 & \alpha_\lambda &= \varepsilon_\lambda
\end{aligned}$$

$$dI_\lambda = -\sigma_a(\lambda) I_\lambda ds = -\rho k_a(\lambda) I_\lambda ds = -k_a(\lambda) I_\lambda du$$

$$\tau_\lambda(z_1, z_2) = \exp\left[-\frac{\int_{z_1}^{z_2} k_a(\lambda) \rho dz}{\mu} \right] = \exp\left[-\int_{u_1}^{u_2} k_a(\lambda) du \right]$$

$$\frac{\mu}{\rho k_e(\lambda)} \frac{dI_\lambda}{dz} = -I_\lambda(\theta, \phi) + \tilde{\alpha}_\lambda B_\lambda(T) + \tilde{\omega}_\lambda < I_\lambda' > \quad < I_\lambda' > = \frac{1}{4\pi} \int_0^{2\pi} \int_1^1 I_\lambda(\mu', \phi') p(\psi_s) d\mu' d\phi'$$

$$\begin{aligned}
\tilde{\alpha}_\lambda &= \frac{\sigma_a(\lambda)}{\sigma_e(\lambda)} & \tilde{\omega}_\lambda &= \frac{\sigma_s(\lambda)}{\sigma_e(\lambda)} & \frac{\mu}{\rho k_e(\lambda)} \frac{dI_\lambda}{dz} &= -I_\lambda(\mu, \phi) + B_\lambda(T)
\end{aligned}$$

$$\begin{aligned}
k_a^L &= \frac{S}{\pi} \frac{\alpha_L}{(\bar{V} - \bar{V}_o)^2 + \alpha_L^2} & \alpha_L(T, p) &= \alpha_L(T_o, p_o) \frac{p}{p_o} \sqrt{\frac{T_o}{T}}
\end{aligned}$$

$$k_a^D = \frac{S}{\alpha_D \sqrt{\pi}} \exp\left[-\frac{(\bar{V} - \bar{V}_o)^2}{\alpha_D^2} \right] \quad \alpha_D(T, \bar{V}_o) = \sqrt{\frac{2kT}{M}} \frac{\bar{V}_o}{c}$$

$$\chi = \frac{2\pi r}{\lambda} \quad Q_s = \frac{k_s}{\pi r^2} \quad \sigma_s = \int_0^\infty \pi r^2 Q_s N(r) dr \quad \sigma_s(\lambda) \cong \frac{8\pi^3}{3\lambda^4} \frac{[n_o(\lambda)^2 - 1]^2}{N_s^2} f(\delta)$$

$$m = n - i n' \quad I_r(\theta_r, \varphi_r) = \int_0^{2\pi} \int_0^{\pi/2} I_i(\theta_i, \varphi_i) \gamma_r(\theta_r, \varphi_r; \theta_i, \varphi_i) \cos \theta_i \sin \theta_i d\theta_i d\varphi_i d\theta_r d\varphi_r$$

$$\gamma_r(\theta_r, \varphi_r; \theta_{sun}, \varphi_{sun}) = \frac{I_r(\theta_r, \varphi_r)}{I_{sun} \Omega_{sun} \cos \theta_{sun}} = \frac{I_r}{E_{sun}}$$

$$A = \frac{M}{E} = \int_0^{2\pi} \gamma_r(\theta_r, \varphi_r; \theta_{sun}, \varphi_{sun}) \cos \theta_r d\Omega_r$$