

Determining the Solar Constant

We can ignore emission to good approx.

$$\frac{dI}{dx} = -I$$

$$\int_{I(0)}^I \frac{dI}{I} = - \int_0^x dx$$

$I(\infty), x=0$

\downarrow

$x \text{ increases}$
 $I \text{ decreases}$

$I(z), x(z)$

z

\vdots

\downarrow

$I(0), x(0)$

$z=0$

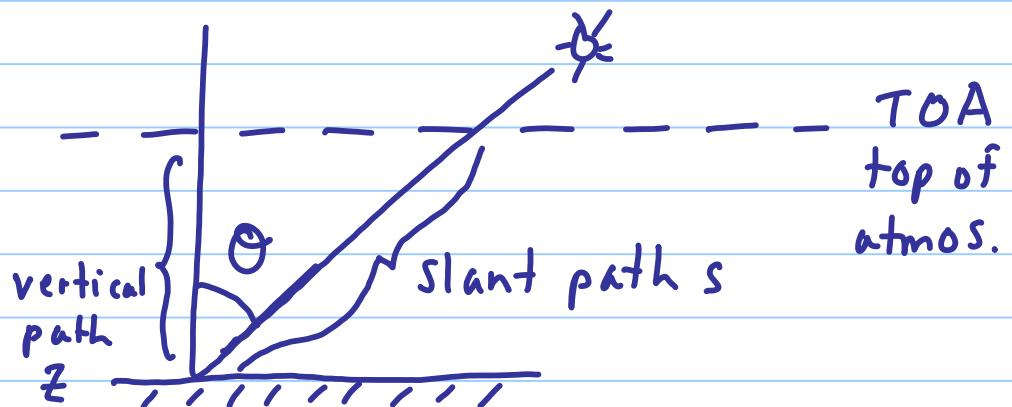
$I = I(\infty) e^{-x}$

$=$

we want to
find $I(0)$

The solar zenith angle between the Sun and the vertical changes during the day so optical depth along the path to the Sun also changes.

Plane parallel atmosphere



$$\cos \theta = z/s$$

$$\therefore s = z / \cos \theta = z \sec \theta$$

Assume that the atmosphere is horizontally homogeneous:

optical depth along slant path = $\chi \sec \theta$

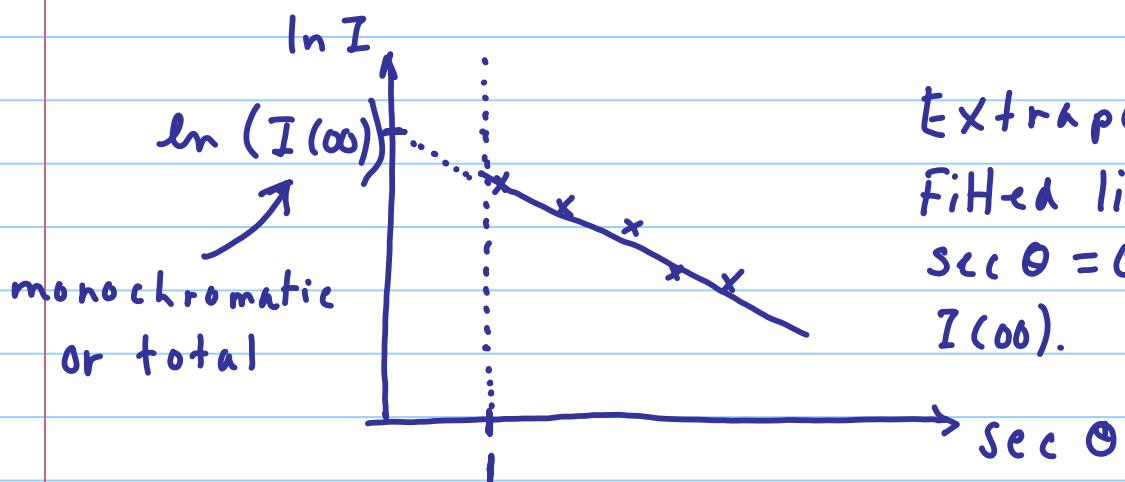
where $\chi = \underline{\text{vertical optical depth}}$

So:

$$I = I(\infty) e^{-\chi \sec \theta}$$

$$\ln I = \ln [I(\infty)] - \chi \sec \theta$$

The SZA θ varies during the day, allowing measurement of I vs. $\sec \theta$.



The total energy in the solar beam is obtained by integrating $I(\infty)$ over all λ and multiplying by the solar solid angle $\Delta \Omega_s$.

\Rightarrow gives total solar energy per second per unit area arriving at the top of the atmosphere \Rightarrow the solar constant

$$S \text{ or } F_s \simeq 1370 \text{ W/m}^2$$

Long method for determining S.

Sources of error:

- ① measurement errors, particularly for energy
- ② as $\theta \uparrow$, energy \downarrow and so errors increase because most instruments have a constant linear error in radiance
- ③ atmospheric variability \rightarrow makes the extrapolation approximate
- ④ scattering of solar radiation out of and into the beam
- ⑤ absorption by gases which makes the atmosphere opaque in some spectral regions

Alternative methods to obtain F_s :

- short method \Rightarrow measure additional parameters to help determine X
- use satellite instruments

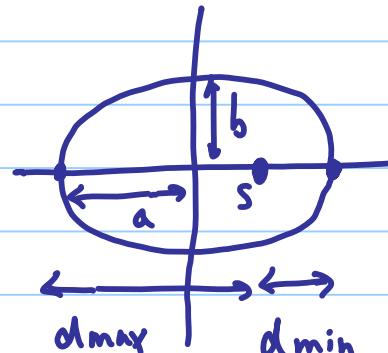
Solar Insolation

Measurements of F_s show that it varies by $\sim 7\%$ over the year

→ due to changing Sun-Earth distance from perihelion (closest, Dec/Jan) to aphelion (furthest, July).

eccentricity of Earth's orbit

$$\begin{aligned} e &= \sqrt{1 - \left(\frac{\text{minor axis}}{\text{major axis}}\right)^2} \\ &= \sqrt{1 - \left(\frac{b}{a}\right)^2} \\ &= 0.017 \end{aligned}$$



$$d_{\min} = (1-e)a = 0.983a$$

$$d_{\max} = (1+e)a = 1.017a$$

solar radiation \propto solid angle subtended
 \propto distance $^{-2}$

$$\frac{\text{max flux density}}{\text{min flux density}} = \left(\frac{1.017}{0.983}\right)^2 = 1.070 \quad \text{G} 7\% \text{ variation}$$

∴ NH receives 7% less/more solar radiation in NH summer (aphelion)/winter (perihelion) than the SH in equivalent seasons.