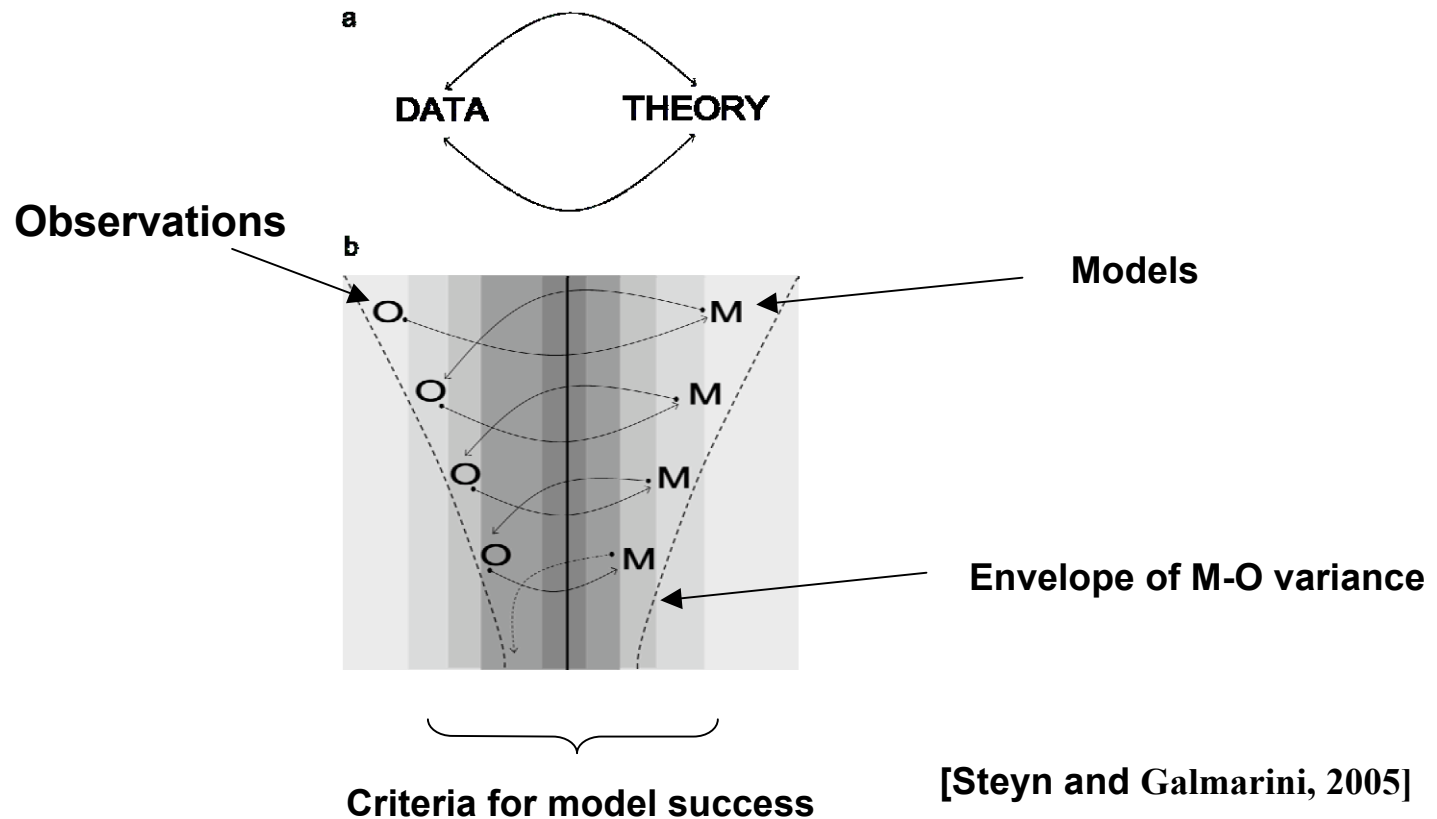


One-Dimensional Models

**GCC Summer School, 2005
Banff, Alberta**

**Dylan Jones
Department of Physics
University of Toronto**

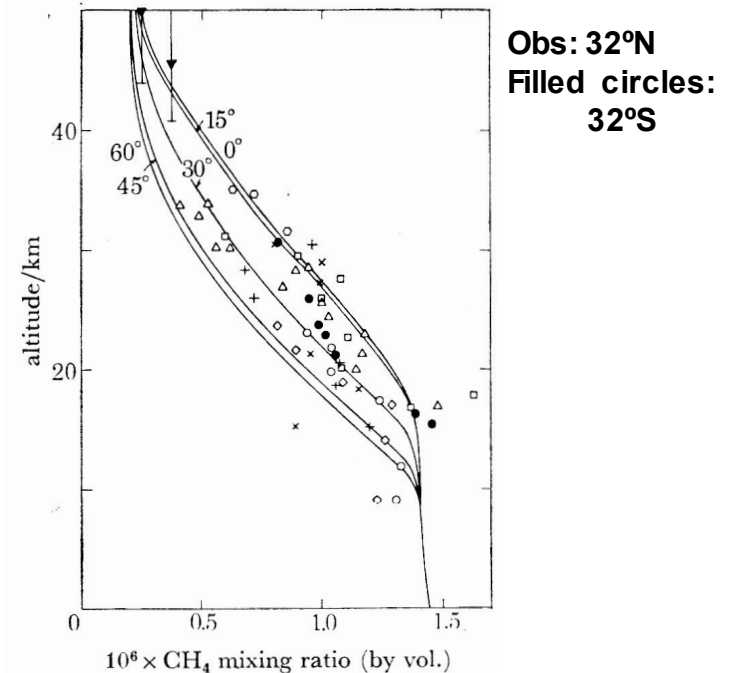
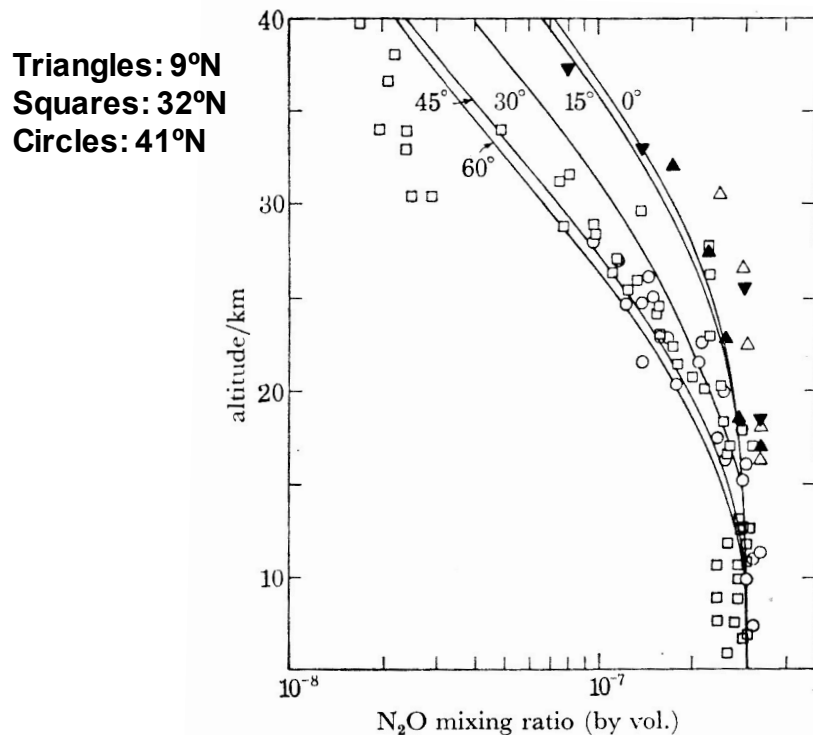
Observations and Models



Choice of model should be guided by quality of observations and desired level of accuracy and precision of understanding or prediction of atmospheric phenomenon

One-dimensional Modelling

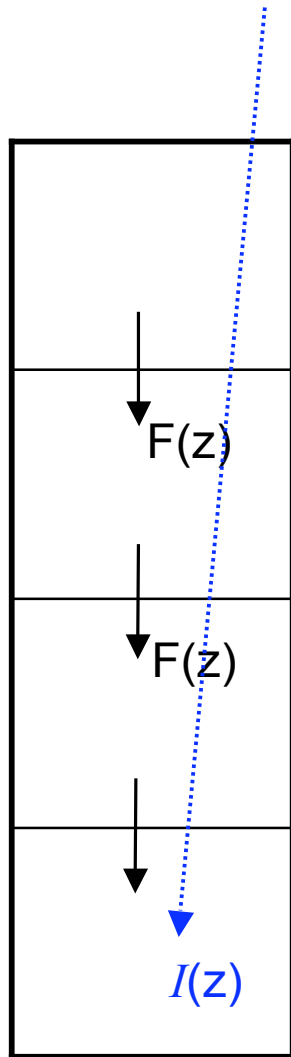
- Due to computational limitations, 1-D models were used extensively for assessments throughout the 1970s and 1980s



[Logan et al., 1978]

- Despite their limitations, 1-D models adequately provided much of our early understanding of the trace constituents in the atmosphere - reflects limited spatio-temporal distribution of data in the pre-satellite era

One-Dimensional Framework



1-D models provide a latitude-longitude averaged (global or hemispheric) representation of the atmosphere

Continuity equation

$$\frac{\partial n(z)}{\partial t} = P - L - \frac{\partial}{\partial z} \left(K(z) M(z) \frac{\partial f(z)}{\partial z} \right)$$

$M(z)$ = atmospheric number density

$n(z)$ = tracer number density

$f(z)$ = tracer mixing ratio

$K(z)$ = vertical

Radiation

$$I(z) = I_0 \exp \left(-\frac{1}{\mu} \int_z^{\infty} \sigma n(z) dz \right)$$

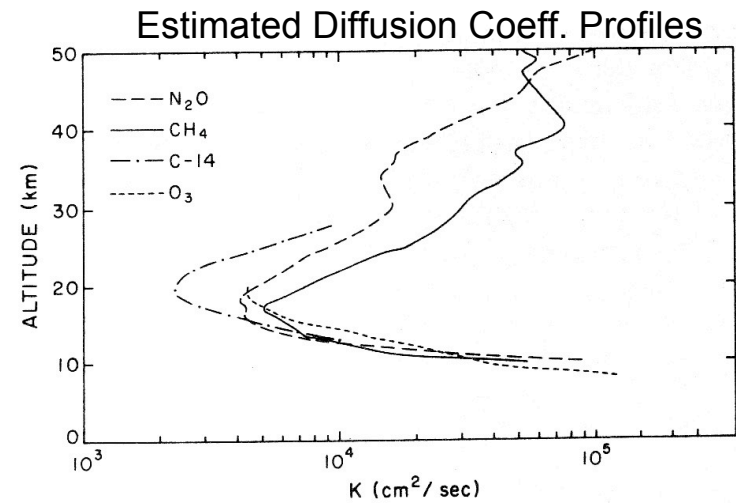
Vertical Diffusion Coefficients

Use observed profiles of trace gases to empirically derive diffusion coefficient

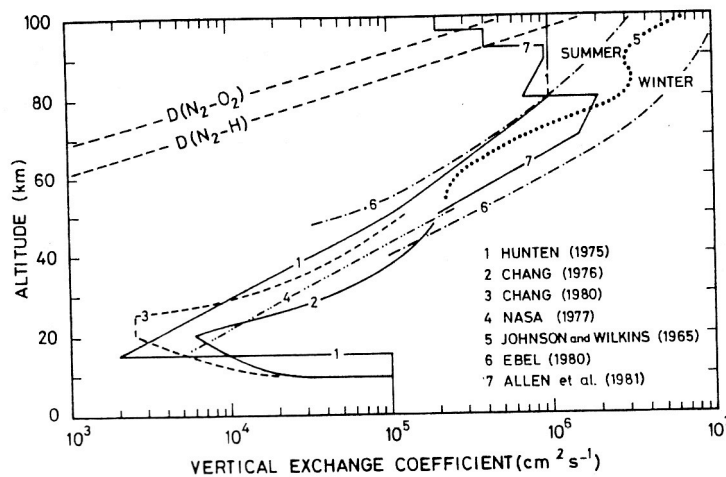
$$\text{vertical flux} = -K(z)M(z)df(z)/dz$$

In steady state

$$K(z) = \left(M(z) \frac{df(z)}{dz} \right)^{-1} \left(\int_z^{\infty} (P(z) - L(z)) dz \right)$$



[Massie and Hunten, 1981]

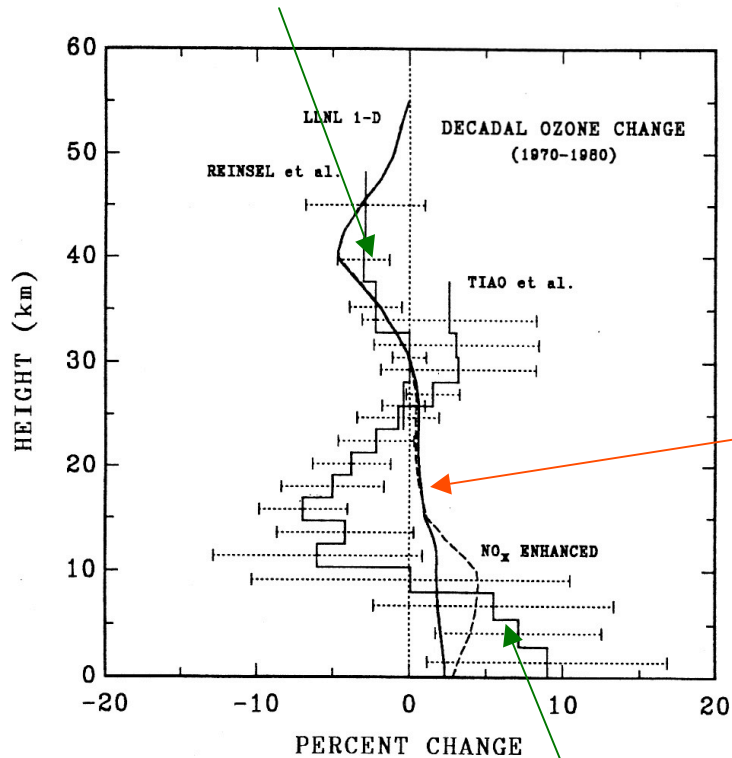


[Brasseur and Solomon, 1986]

K profiles used in a range of 1-D models in 1960s, 1970s and 1980s

Stratospheric Ozone Trends

Umkehr measurements



[Lacis et al, 1990]

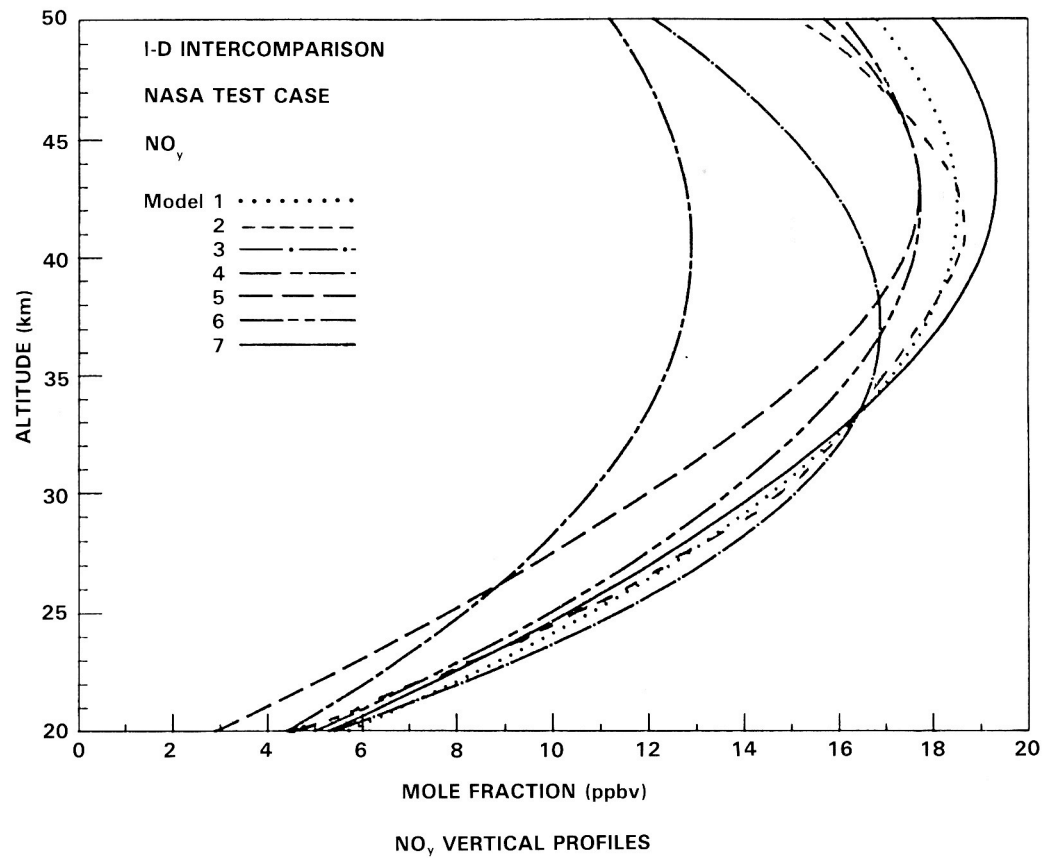
NH ozonesondes

- The 1-D model suggested a slight increase in O₃ in the lower stratosphere due to CFC increases

1-D model

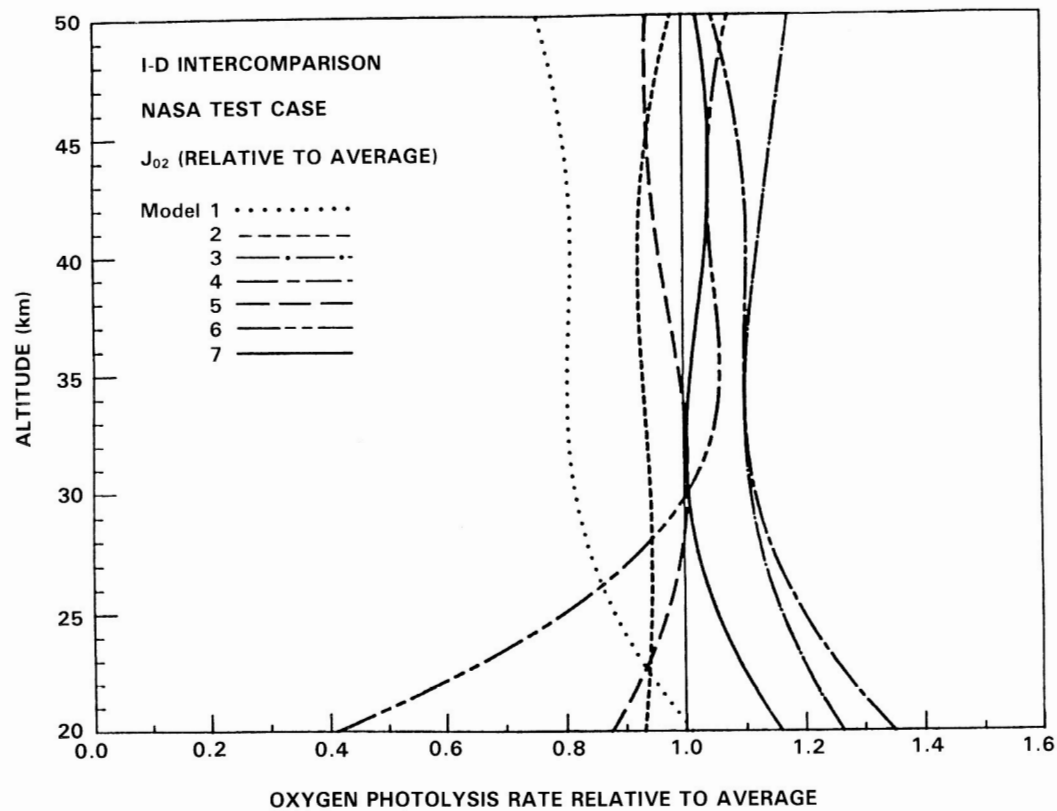
- Discrepancy reflects the inability of the 1-D model to account for the effects of atmospheric transport

Comparison of NO_y in 1-D Models



[WMO, 1985]

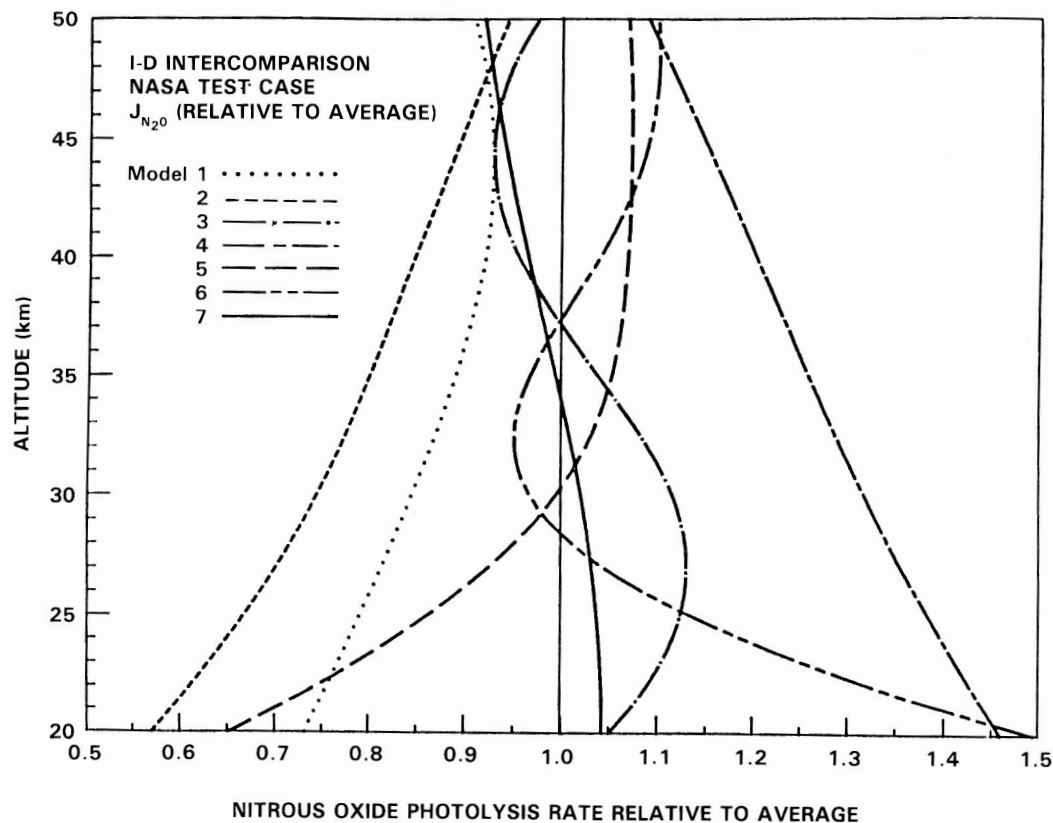
Comparison of O₂ Photolysis in 1-D Models



[WMO, 1985]

Photolysis of N₂O occurs in the region 173-240 nm ⇒ sensitive to Schumann-Runge bands (and Herzberg continuum) of O₂

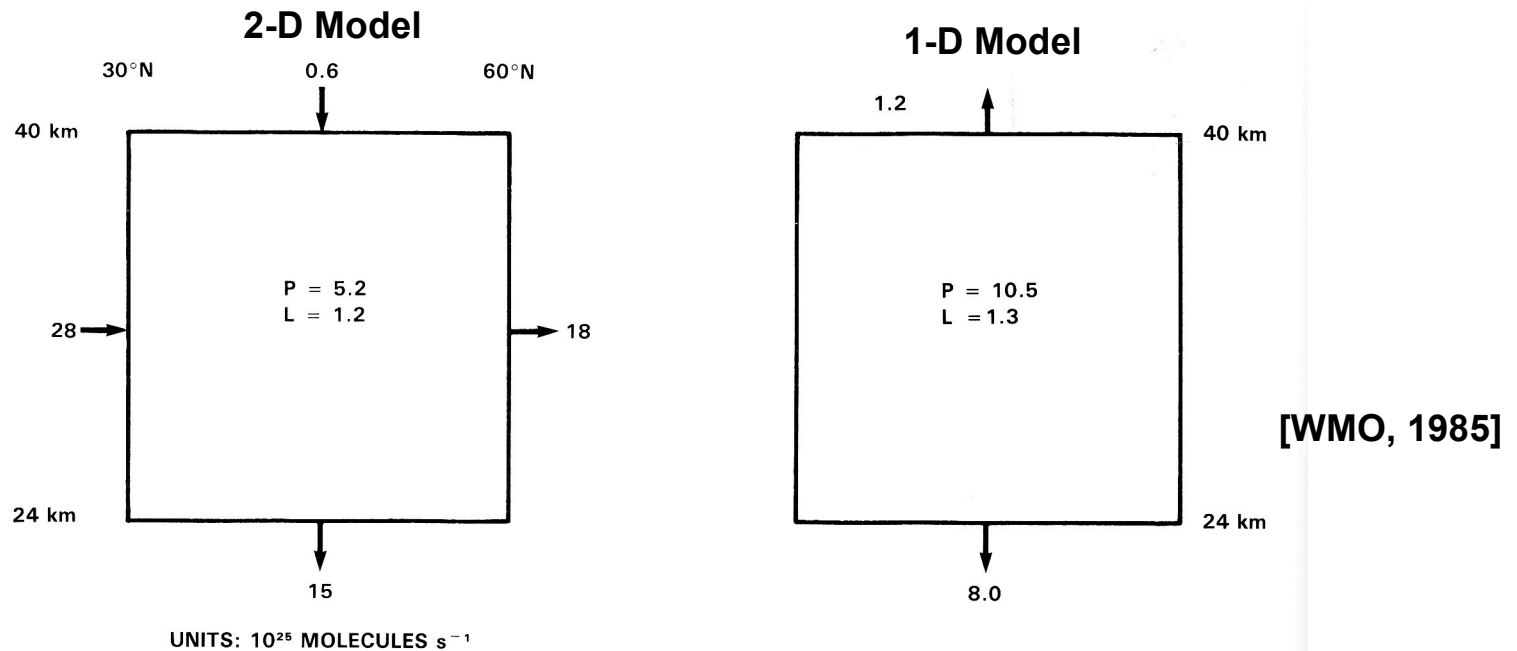
Comparison of N₂O Photolysis in 1-D Models



[WMO, 1985]



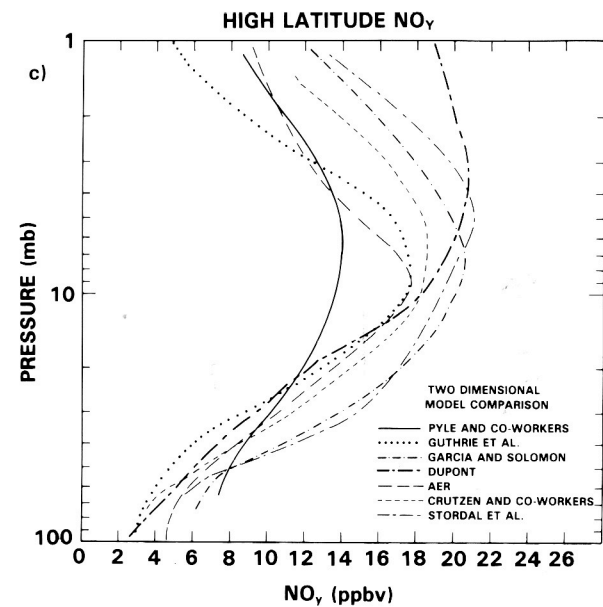
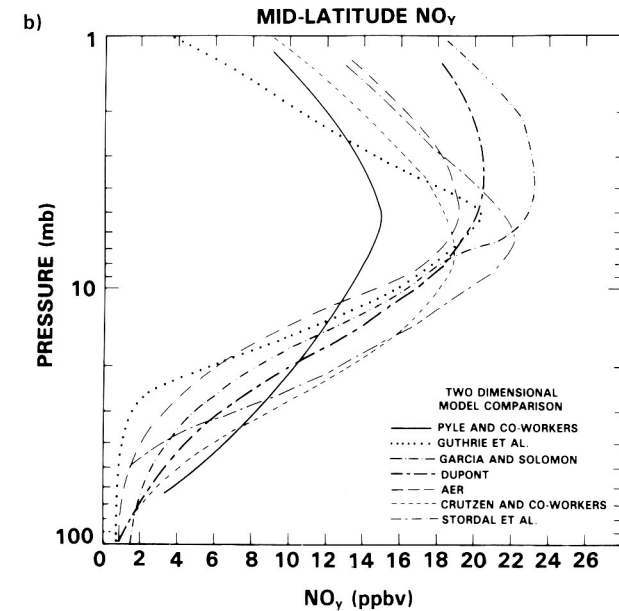
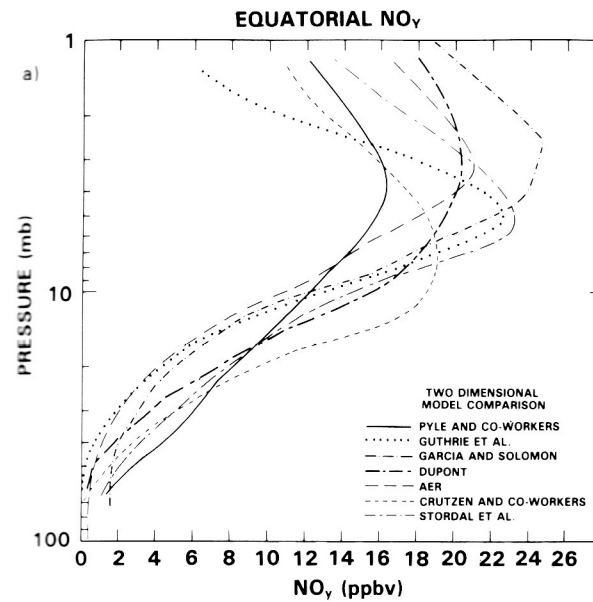
Comparison of NO_y budget in 1-D and 2-D Models



- In 2-D framework, meridional transport from source region in tropics important
- in 1-D model, balance is between in situ production (P) and vertical diffusive transport

Comparison of NO_y in 2-D Models

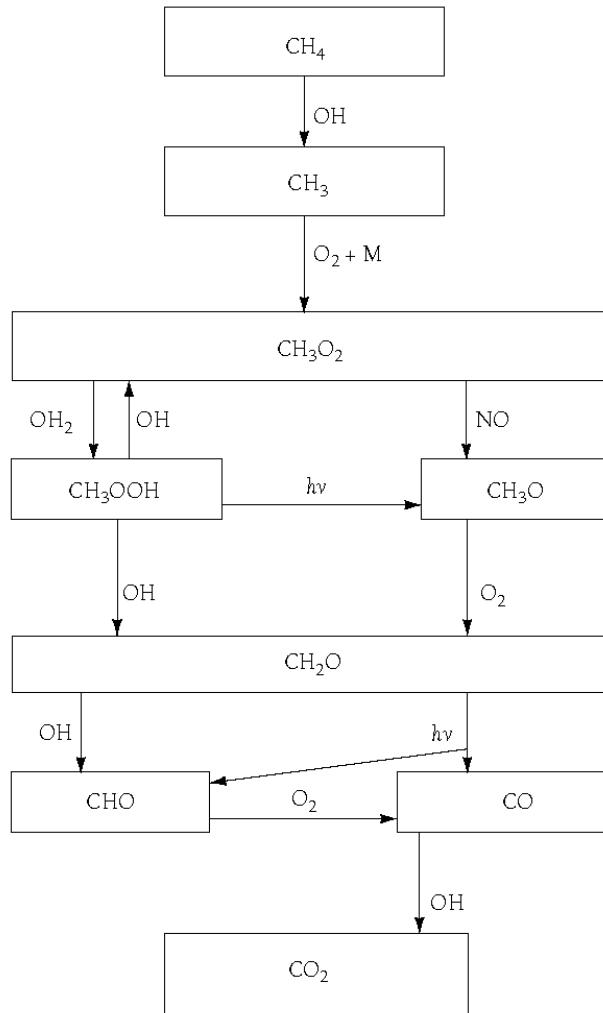
- In 1985 there were large differences in NO_y also in the 2-D models
- At present, the discrepancies in NO_y between models (2-D and 3-D) is not much better



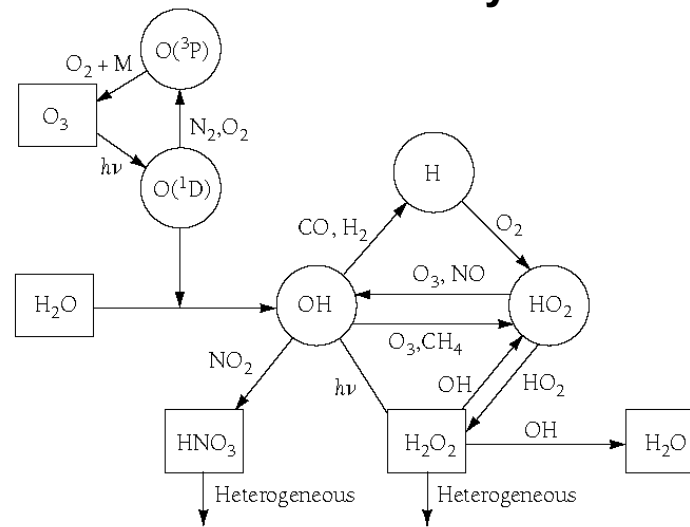
[WMO, 1985]

Tropospheric chemistry

Methane Oxidation

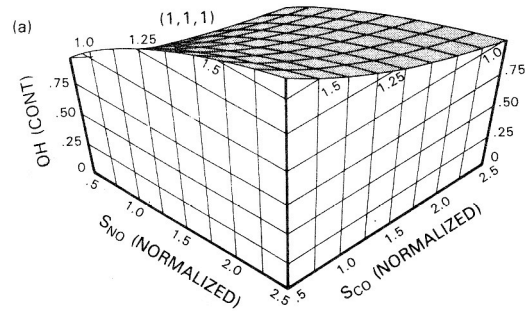


HOx Cycle



[M. B. McElroy, 2002]

Sensitivity of tropospheric OH to changes in emissions of NO and CO



Continental

$$S_{\text{NO}} = 8 \times 10^9 \text{ cm}^{-2}\text{s}^{-1}$$

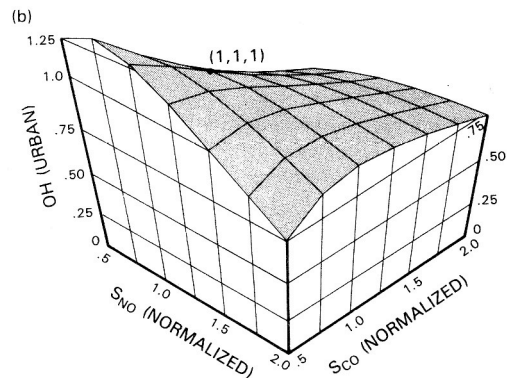
$$S_{\text{CO}} = 2.0 \times 10^{11}$$

$$S_{\text{CH}_4} = 6.5 \times 10^{10}$$

$$[\text{NO}_x] = 0.2 \text{ ppb}$$

$$[\text{CO}] = 130 \text{ ppb}$$

$$[\text{CH}_4] = 1.7 \text{ ppm}$$



Urban

$$S_{\text{NO}} = 7 \times 10^{10} \text{ cm}^{-2}\text{s}^{-1}$$

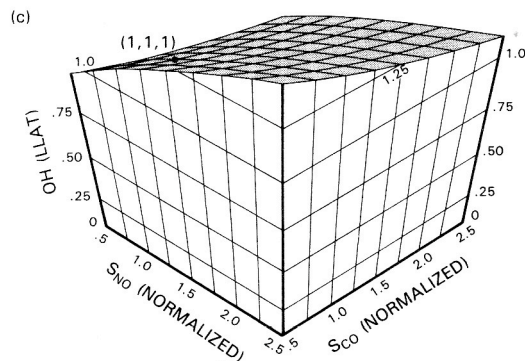
$$S_{\text{CO}} = 8.0 \times 10^{11}$$

$$S_{\text{CH}_4} = 7.8 \times 10^{10}$$

$$[\text{NO}_x] = 1.4 \text{ ppb}$$

$$[\text{CO}] = 380 \text{ ppb}$$

$$[\text{CH}_4] = 1.7 \text{ ppm}$$



Low Latitude

$$S_{\text{NO}} = 6.7 \times 10^8 \text{ cm}^{-2}\text{s}^{-1}$$

$$S_{\text{CO}} = 1.2 \times 10^{11}$$

$$S_{\text{CH}_4} = 1.0 \times 10^{11}$$

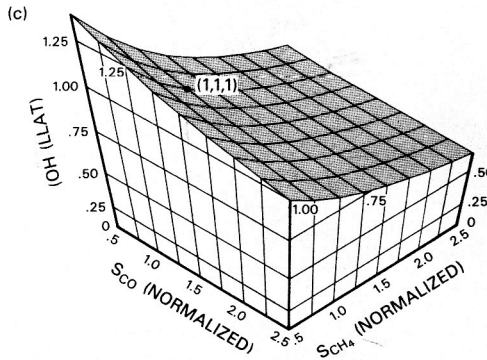
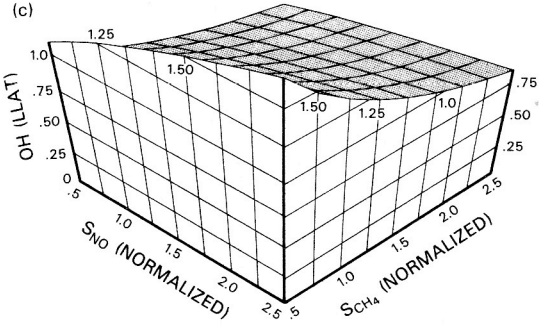
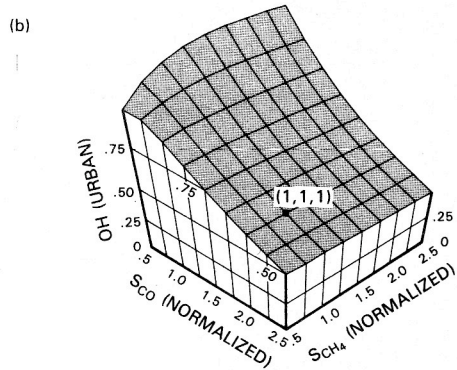
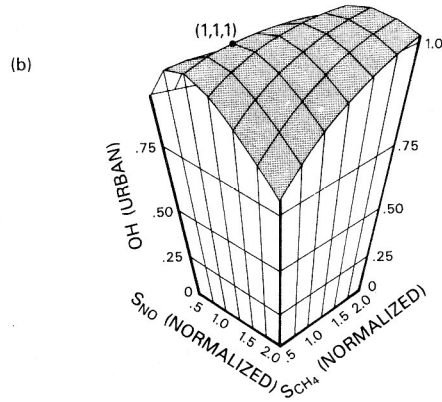
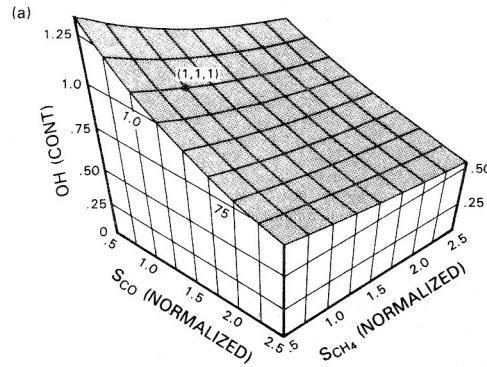
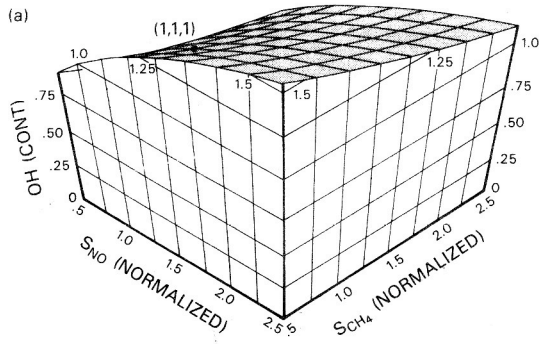
$$[\text{NO}_x] = 0.024 \text{ ppb}$$

$$[\text{CO}] = 89 \text{ ppb}$$

$$[\text{CH}_4] = 1.7 \text{ ppm}$$

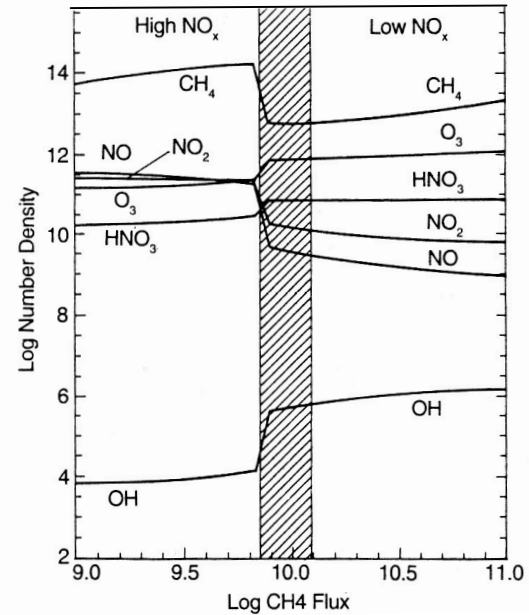
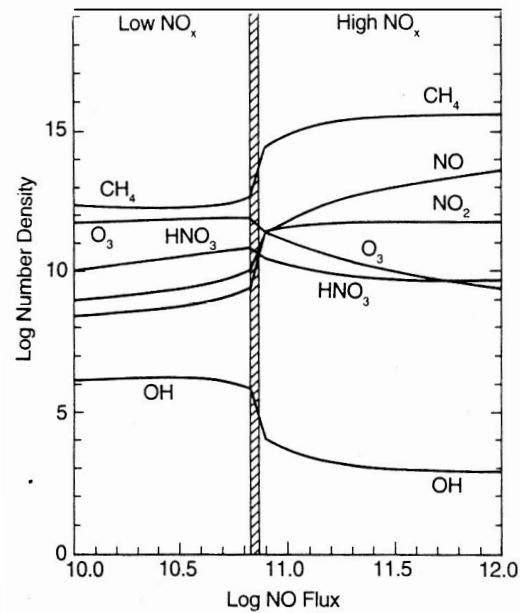
[Thompson et al., 1989]

Sensitivity of tropospheric OH to changes in emissions of NO and CH₄



CH₄-HO_x-NO_x-CO
chemistry nonlinear

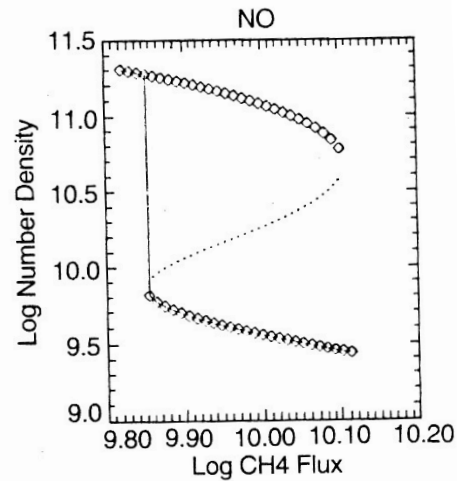
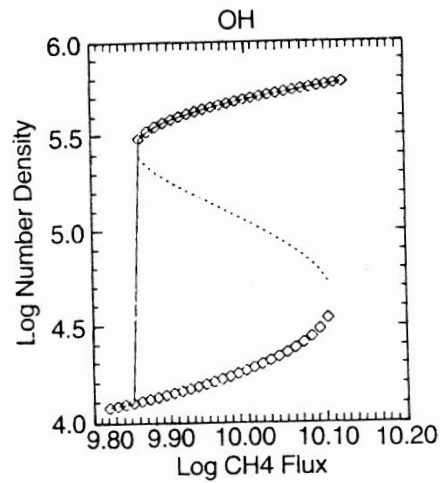
Instability in the $\text{CH}_4\text{-NO}_x\text{-O}_x\text{-HO}_x$ Chemical System (in a Box Model)



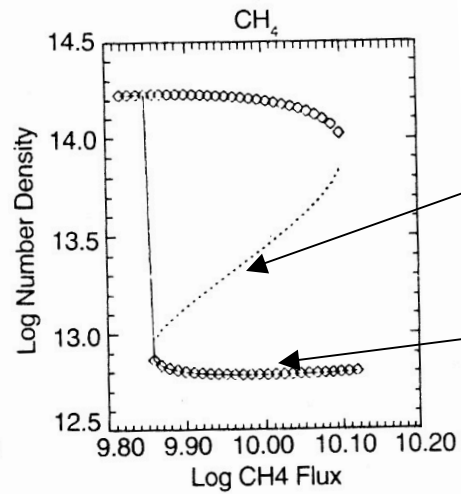
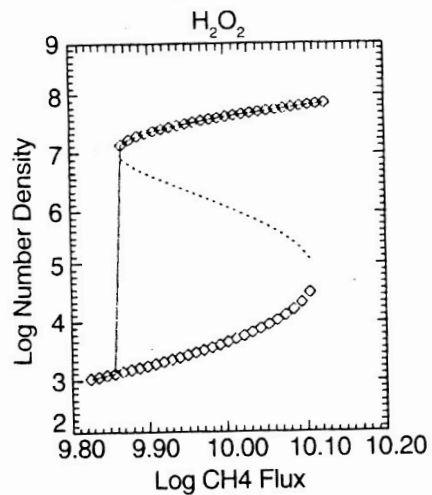
[Stewart, 1993]

Abrupt transition between states characterized by low and high abundances of NO_x

Multiple Steady States

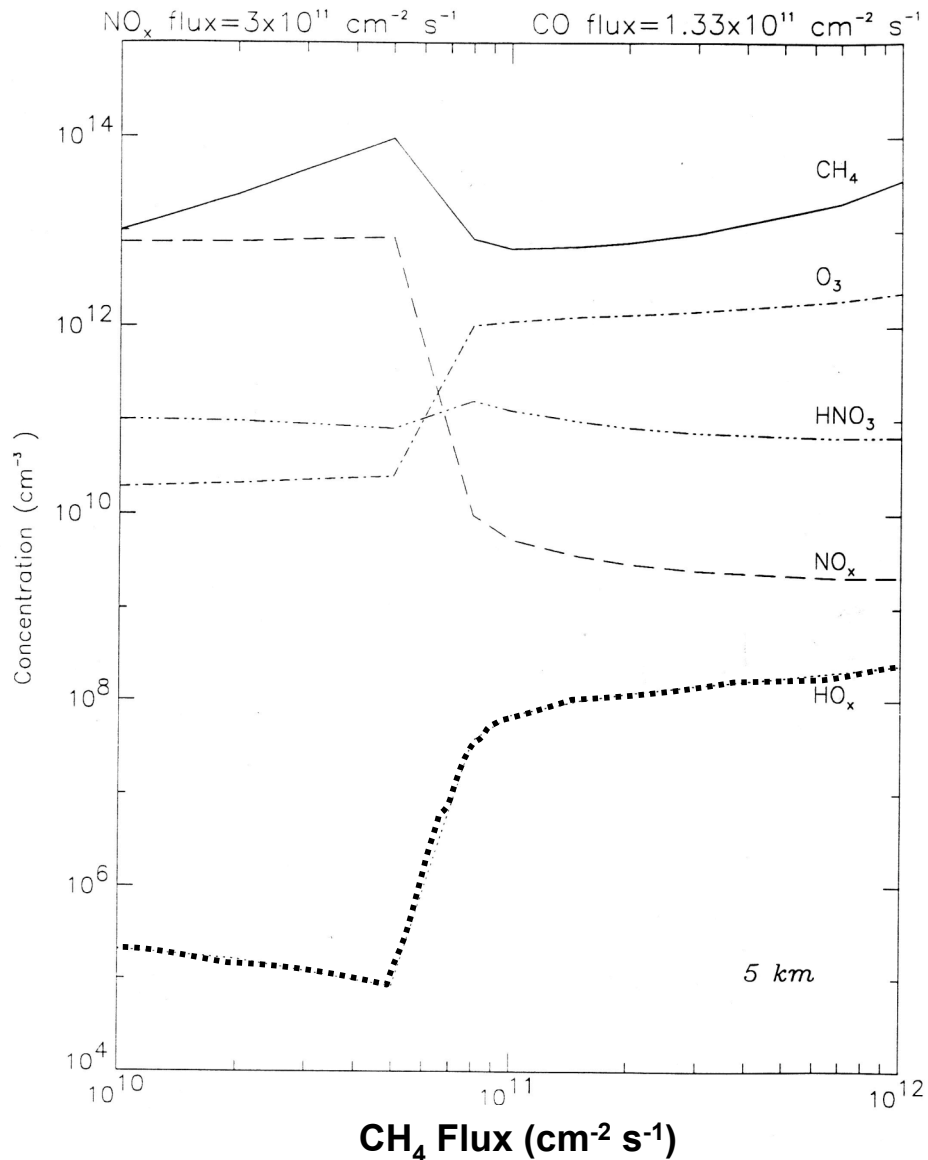


Existence of MSS sensitive to abundance of other tracers e.g. no MSS if RH < 40%



[Stewart, 1993]

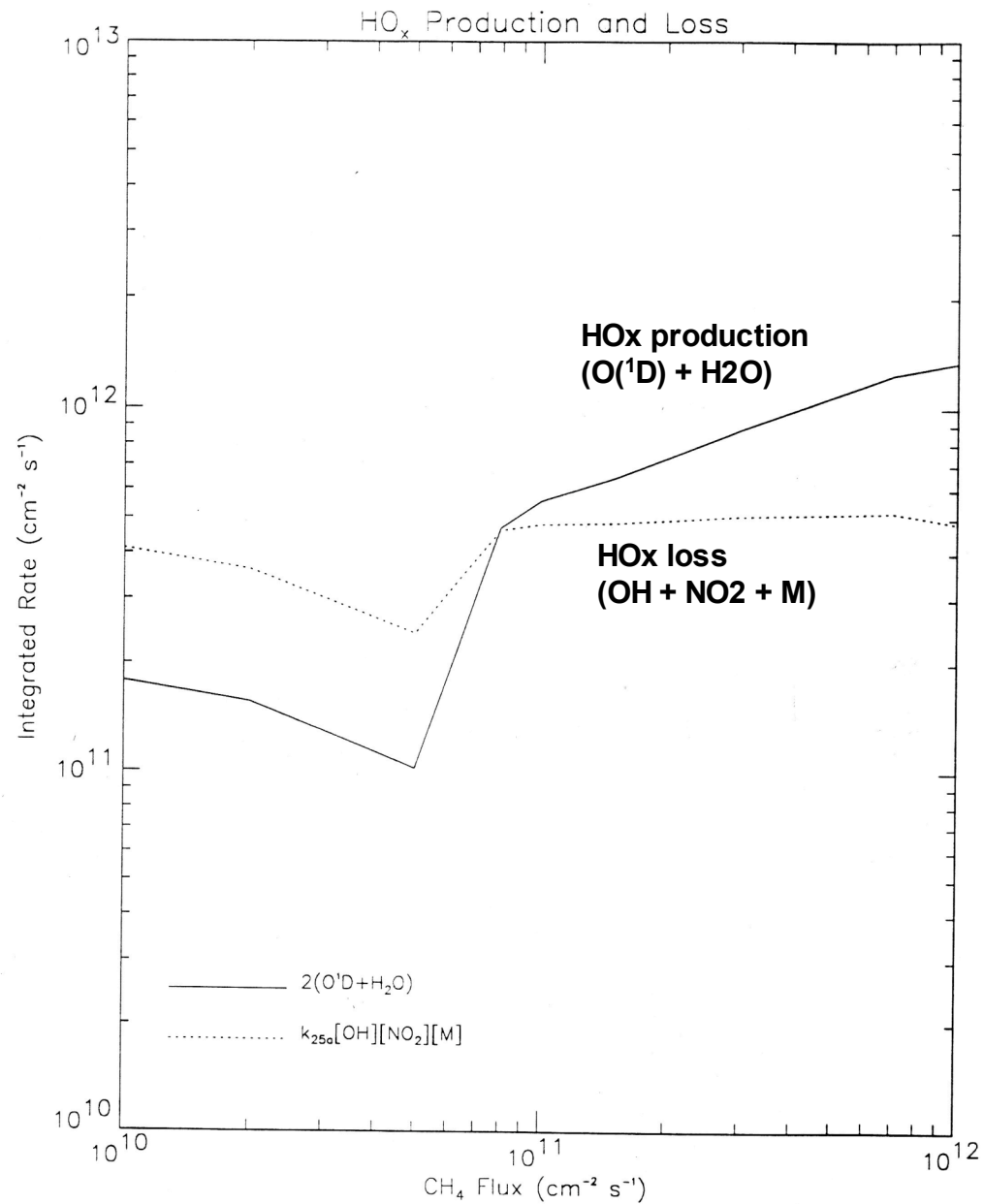
1-D Simulation of Stewart's Results



- Decreasing CH_4 emissions results in a transition to a high NO_x regime
- Total O_3 column decreases by a factor of 3 from the low to high NO_x regime (NO_x in lower strat ≈ 0.5 ppm)

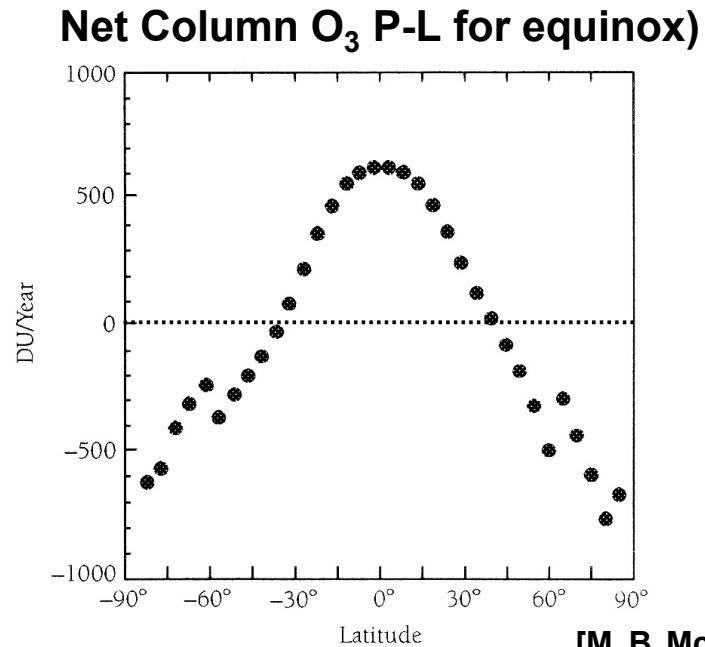
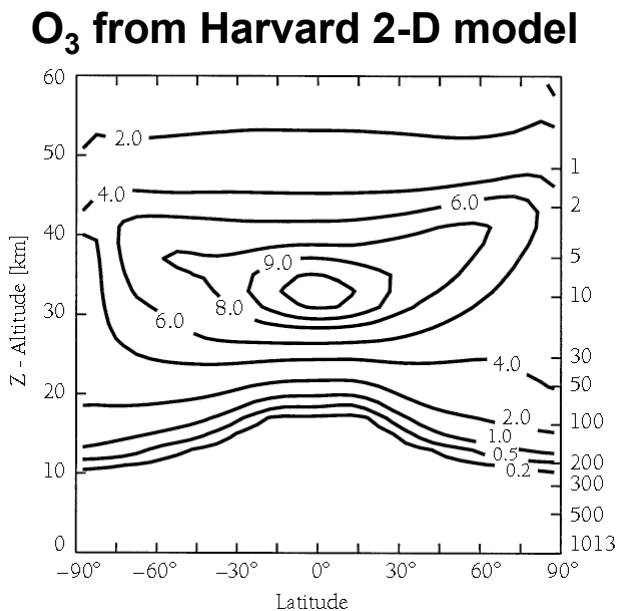
- Results suggest the possibility of MSS in the 1-D model
- These abrupt transitions were not found in the 2-D model
- A more detailed search of state space is needed for the 1-D and 2-D models

HO_x Production and Loss



At low levels of CH₄, OH production is insufficient to support HNO₃ formation
⇒ NO_x concentrations increase dramatically

Influence of Transport on Stratospheric O₃



[M. B. McElroy, 2002]

- **Net O₃ production in tropical stratosphere reflects large flux of UV photons**
- **At high levels of CH₄, oxidation shifts to tropical stratosphere which helps stabilize the system**

A More Dynamically Consistent Approach

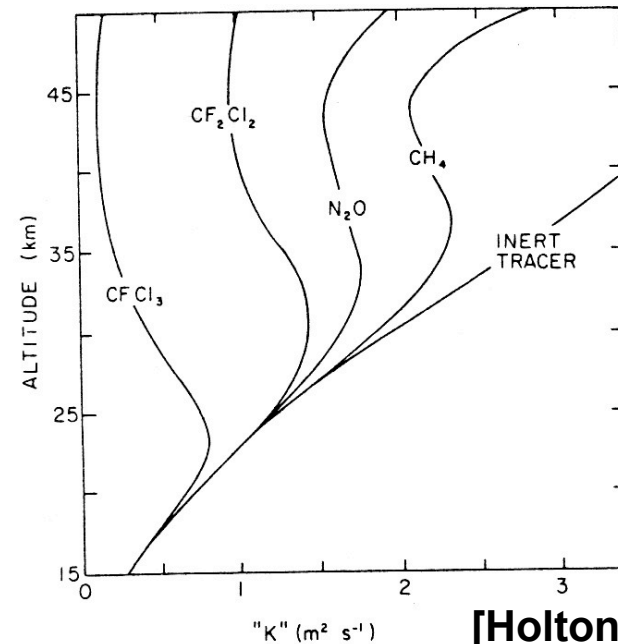
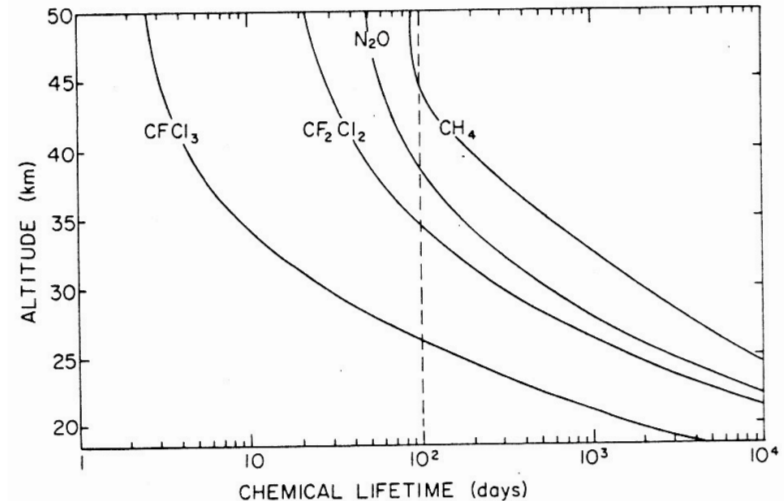
Approximate the transport with a vertical
“eddy transport” coefficient

$$K = \frac{W_2^2}{5(\tau_c^{-1} + \tau_d^{-1})}$$

$$W_2 = RQ_2 / (N^2 H)$$

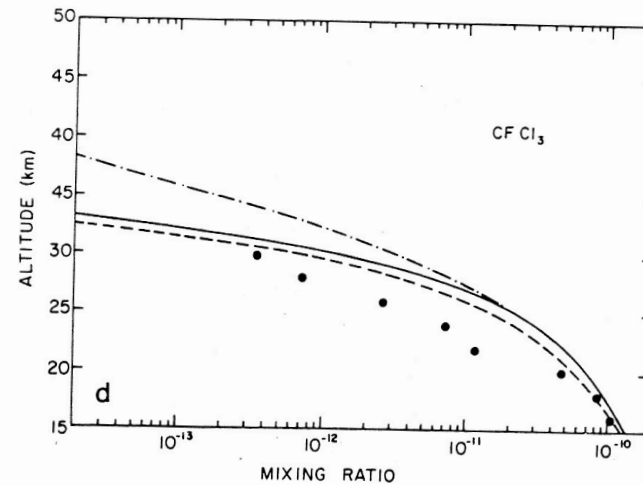
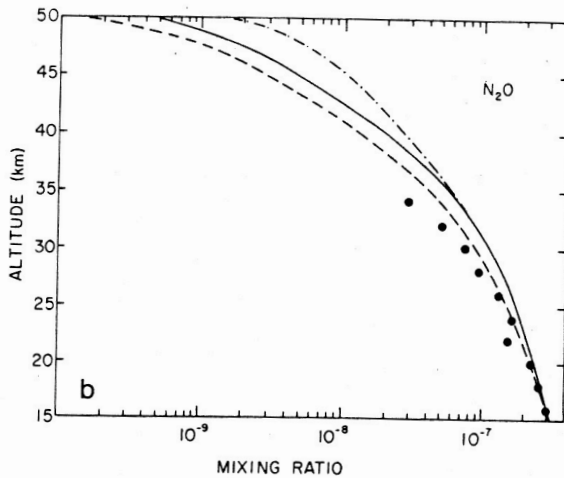
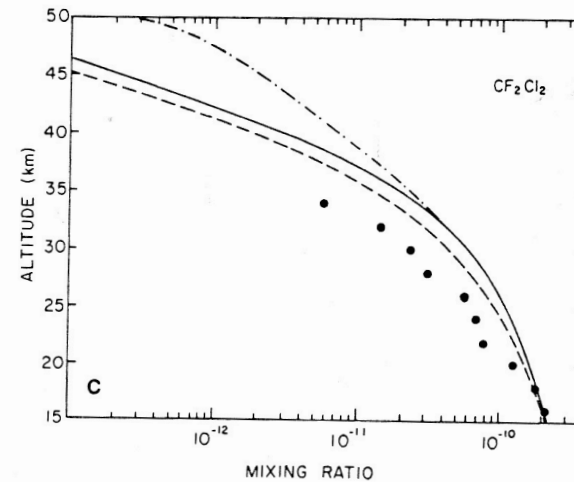
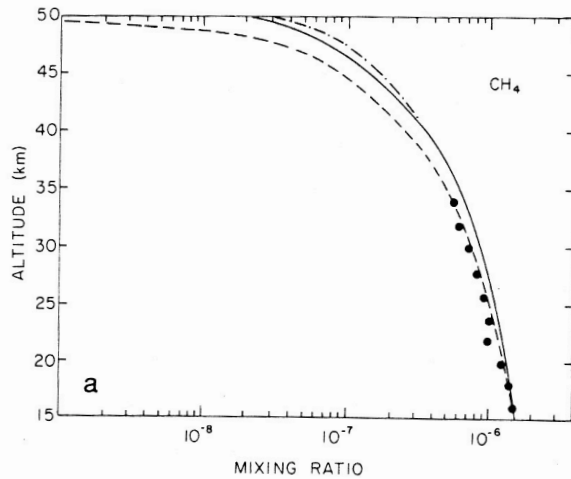
- W_2 = vertical mass circulation
- Q_2 is annual mean diabatic heating rate projected on $P_2(\mu)$
- τ_c = timescale for the chemistry
- τ_d = timescale for horizontal eddy mixing

Vertical transport coefficient species-specific



[Holton, 1986]

Sensitivity of Tracer Profile to K_z



- Filled circles: Observations at 44°N
- Dashed-dotted line: global mean with K_z for inert tracer
- Solid line: global mean for species specific K_z
- Dashed line: simulated profiles for 45°N

[Holton, 1986]

Main Points of Lecture

- **1-D chemical-radiative-diffusive models were used extensively in 1970s and 1980s**
- **Modelling the vertical advective transport as a diffusive process provides a fundamentally flawed simulation of the distribution of the trace gases \Rightarrow one K does not fit all**
- **More dynamically consistent approaches (e.g. Holton [1985]) were proposed but never adopted widely**
- **Despite these limitations, 1-D models provided much of our understanding of the trace constituents in the atmosphere during the pre-satellite era**
- **1-D chemical-radiative models are currently used in 3-D model - e.g., domain decomposition for parallel numerical simulations**
- **The limitations of 1-D models reflects importance of the meridional transport of tracers in the atmosphere \Rightarrow Brewer-Dobson circulation**